NDU MAT 224

Calculus IV

Exam #2

December 7, 2016

Duration: 60 minutes

	Problem Number	Points	Score
Name:	1	40	/
	2	17	
Section:	3	29	
Instructor:	4	20	
Grade:	Total	106	

1) (40 points) For each of the following multiple-choice questions, circle the <u>letter</u> of the correct answer. If more than one letter is circled in the same problem, you will receive no credit for that problem.

Question A:

$$\int_{-1}^{1} \int_{0}^{\sqrt{1-y^2}} e^{2x^2+2y^2} dx dy =$$

a)
$$\frac{\pi}{2}(e^2-1)$$

b)
$$\frac{\pi}{4}(e^2-1)$$

c)
$$\frac{\pi}{8}(e^2-1)$$

d)
$$\frac{\pi}{16}(e^2-1)$$

Question B:

$$\int_{0}^{4} \int_{\sqrt{y}}^{2} \cos(x^{3} + 1) \, dx dy =$$

a)
$$\frac{\sin(1) - \sin(9)}{3}$$

b)
$$\sin(9) - \sin 1$$

c)
$$\frac{\sin(9) - \sin(1)}{3}$$

d)
$$\sin(1) - \sin(9)$$

Question C: The value of the integral $\int_{0}^{1} \int_{-\sqrt{1-x^2}}^{\sqrt{1-x^2}} \int_{-\left(x^2+y^2\right)}^{\left(x^2+y^2\right)} 21xy^2 dz dy dx \text{ is:}$

- a) 4
- b) -4
- c) 2
- d) -2

Question D:

The volume of the region cut from the first octant by the plane 2x + y + z = 4 can be calculated using the integral:

a)
$$\int_{0}^{4} \int_{0}^{4-z} \int_{0}^{4-2x-z} dy dx dz$$

b)
$$\int_{0}^{4} \int_{0}^{2-y/2} \int_{0}^{4-2x-y} dy dx dz$$

c)
$$\int_{0}^{4} \int_{0}^{2} \int_{0}^{2-z/2-x} dy dx dz$$

d)
$$\int_{0}^{4} \int_{0}^{2-z/2} \int_{0}^{4-z-2x} dy dx dz$$

Question E:

Using the method of Lagrange Multipliers to find the point closest to the origin on the curve of intersection of the plane x + y + z = 1 and the cone $z^2 = 2x^2 + 2y^2$, can yield the system of equations:

a)
$$2x = \lambda + 4\mu x$$
$$2y = \lambda + 4\mu y$$
$$2z = \lambda - 2\mu z$$
$$x + y + z - 1 = 0$$
$$2x^{2} + 2y^{2} - z^{2} = 0$$

b)
$$2x = \lambda + 4\mu x$$

 $2y = \lambda + 4\mu y$
 $2z = \lambda$
 $x + y + z - 1 = 0$

$$2x = \lambda + 4\mu x \qquad b) \ 2x = \lambda + 4\mu x \qquad c) \ 2x = \lambda + 4\mu x \qquad 2y = \lambda + 4\mu y \qquad 2y = \lambda + 4\mu y \qquad 2y = \lambda + 4\mu y \qquad 2y = 4\mu y \qquad 2z = \lambda - 2\mu z \qquad 2z = \lambda \qquad 2z$$



2) (17 points) Find all local extreme values and saddle points of the function $f(x,y) = x^4 - 8x^2 + 3y^2 - 6y$.



- 3) (29 points) Consider the solid region D that lies inside the cylinder $x^2 + y^2 = 1$, bounded from below by the paraboloid $z = 1 x^2 y^2$ and from above by the plane z = 4.
- a) (4 points) Draw the region D.

- b) (25 points) Set up triple integrals representing the volume of the region D:
 - i) (10 points) In cylindrical coordinates with the order of integration $dz dr d\theta$.

ii) (15 points) In cylindrical coordinates with the order of integration $dr dz d\theta$.



- 4) (20 points) Let D be the region bounded below by the xy-plane, on the sides by the sphere $x^2 + y^2 + z^2 = 4$, and above by the cone $z = \sqrt{x^2 + y^2}$.
 - a) (4 points) Draw the region D.

b) (16 points) Set up triple integrals representing the volume of the region D in cylindrical coordinates in the order $dz dr d\theta$.